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274002710

CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/52

Paper 5 Investigation (Core)

February/March 2024

1 hour 10 minutes

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.

INFORMATION

- The total mark for this paper is 36.
- The number of marks for each question or part question is shown in brackets [].

This document has 8 pages.

Answer **all** the questions.

INVESTIGATION

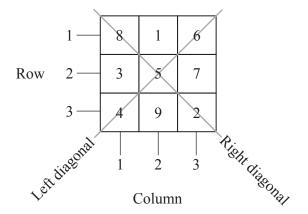
MAGIC SQUARES

This investigation looks at ways to make a magic square. A magic square is a grid with a different number in each square.

The numbers in each row, each column or each diagonal all add up to the same total. This is the *line total*.

Example

This is a 3 by 3 magic square using the integers 1 to 9. The line total is 15.



Line totals

Row 1	8 + 1 + 6 = 15	Column 1	8 + 3 + 4 = 15	Left diagonal	4+5+6=15
Row 2	3+5+7=15	Column 2	1 + 5 + 9 = 15	Right diagonal	8 + 5 + 2 = 15
Dow 2	4 + 0 + 2 = 15	Column 2	6 + 7 + 2 = 15		

1 This is part of a different 3 by 3 magic square using the integers 1 to 9.

2	9	4
7		3
	1	

(a) Work out the line total for this magic square.

.....[2]

(b) Complete this magic square.

[3]

A and B are two magic squares using the integers 1 to 9. More magic squares can be made using reflection.

B is made by reflecting the position of each integer using a vertical line of reflection.

The line of reflection goes through the middle column of A.

The numbers move from the square in A to the reflected square in B.

	A	
8	1	6
3	5	7
4	9	2

	ı	
8-	1	- 6
3	5	7
4	9	2

	В	
6	1	8
7	5	3
2	9	4

Line of reflection

(a) Draw a horizontal line of reflection through the middle row of magic square A.

Complete the new magic square C using the horizontal line of reflection.

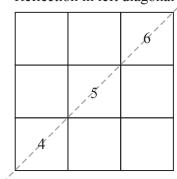
	С	
3	5	7

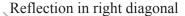
[1]

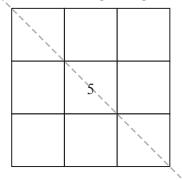
(b) Two different magic squares can be made by reflection in the left and right diagonal lines drawn on A.

Complete these magic squares.

Reflection in left diagonal







[2]

3 (a)	(i)	Calculate	the	total	of the	integers	1	to	9.
• (.,	\ - /	Carcarace	CIIC	count	OI UIIO	111105015	-	•	_

		[1]
	(ii)	A 3 by 3 magic square uses the integers 1 to 9.
		Complete the following statements to find the line total for this magic square.
		The total of the integers in all three rows =
		The line total \div \div $=$ $[2]$
(b)	In a	ll of the magic squares using the integers 1 to 9 the integer in the middle square is the same.
	(i)	Write down the integers 1 to 9.
	(ii)	What is the connection between the middle integer of the integers 1 to 9 and the magic square?
		[1]
	(iii)	Explain how to use the middle integer of the integers 1 to 9 to find the line total of a 3 by 3 magic square.
		[1]

4

A 3	by 3	magic square is made using	g the eve	n integer	rs from 2	to 18.	
(a)	(i)	Find the middle integer of	these in	tegers.			
	(ii)	Use your answer to Quest	tion 3(b)	(iii) to fir	nd the lir	ne total for this magic square.	[2]
							[1]
(iii)	Use your answers to part	(i) and p	art (ii) to	o help yo	ou complete the magic square below.	
			16		12		
							[2]
(b)	Use	your answer to part (a)(iii) and a re	eflection	to make	another 3 by 3 magic square.	

[1]

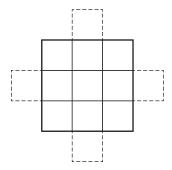
5 This is a method to make a 3 by 3 magic square.

Example

This uses the integers 1 to 9.

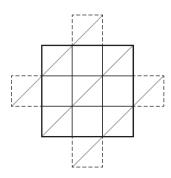
Step 1

Add one square to each edge to make a cross shape.



Step 2

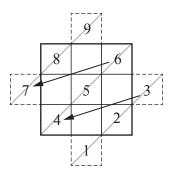
Draw three diagonals on the grid. Each one goes through three squares.



Step 3

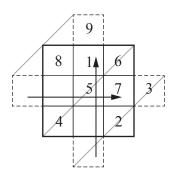
Write the smallest integer in the bottom square.

Write the other integers along the diagonals in order, as shown.



Step 4

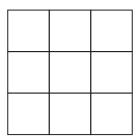
Move the integers from the outside squares to the empty squares inside and opposite.



Completed magic square

8	1	6
3	5	7
4	9	2

(a) (i) Use the method to make a 3 by 3 magic square using the integers 15 to 23.



[4]

(ii) Work out the line total.

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	11	
	- I	

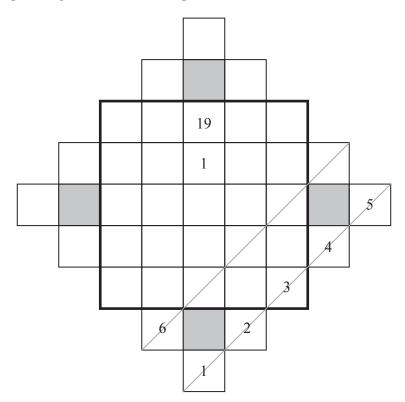
(b) (i) You can use a similar method to make a 5 by 5 magic square using the integers 1 to 25. Two of the diagonals through 5 squares have been drawn.

The first six integers have been placed on the correct diagonals.

Complete the 5 by 5 magic square.

The integers 1, 3 and 19 have been put in their final positions to help you.

Do **not** put integers in the shaded squares.



[5]

(ii) Complete this statement.

The line total is \times middle integer. [2]

Different 3 by 3 magic squares are made using the first nine terms of a sequence.

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The first term of the sequence is 2. The *n*th term of the sequence is 3n-1.

Find four of these magic squares. Use the method of **Question 5** and reflection to help you.

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[4]

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